

TYPE 1 (conj. ACID of a weak base)

(only the SALT of a weak base is put in solution)

For a salt, BHX, of the weak base (B) in water:



Note that BH^+ behaves EXACTLY like a weak acid in water (a Type 1 problem for acids) and the equilibria is



$$K_a = \frac{[\text{H}^+][\text{B}]}{[\text{BH}^+]}$$

member K_a for BH^+ must be calculated from K_b for B: $K_a = \frac{K_w}{K_b}$

Now let C_{BH^+} be the analytical concentration (label) of the conjugate acid, BH^+ :
Our Equilibrium "Chart"

	$[\text{BH}^+]$	$[\text{H}^+]$	$[\text{B}]$
initial	C_{BH^+}	0	0
change	$-x$	$+x$	$+x$
final	$C_{\text{BH}^+} - x$	x	x

$$K_a = \frac{x^2}{(C_{\text{BH}^+} - x)} \quad \text{Equation 3.1}$$

$$K_a C_{\text{BH}^+} - K_a(x) = x^2$$

$$0 = x^2 + K_a(x) - K_a C_{\text{BH}^+}$$

$$[\text{H}^+] = [\text{B}] = x = \frac{-K_a + \sqrt{K_a^2 + 4K_a C_{\text{BH}^+}}}{2}$$

This equation is the exact solution for calculating the $[\text{H}^+]$ for any solution made by mixing a concentration of ONLY a conjugate weak acid, BH^+ , in water.

If we are using a REASONABLE concentration for BH^+ (somewhere between 1.0 M and 0.05 M) AND K_a is small enough (say less than 10^{-4}) we can make the following assumption:

$$C_{\text{BH}^+} - x \cong C_{\text{BH}^+} \quad \text{all this is saying is that } x \text{ is so small compared to } C_{\text{BH}^+}, \text{ it doesn't change it}$$

$$K_a = \frac{x^2}{C_{\text{BH}^+}}$$

and solving:

$[\text{H}^+] = [\text{B}] = x = \sqrt{K_a C_{\text{BH}^+}}$	Equation 3.2
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This equation is the approximate solution for calculating the $[\text{H}^+]$ for any conjugate acid, BH^+ , of the weak base, B, where $K_b < 10^{-4}$. Although it's approximate, it will be close enough (accurate to 2 or 3 significant figures) to use this MOST of the time.